

1. Find the required information and graph the conic section:

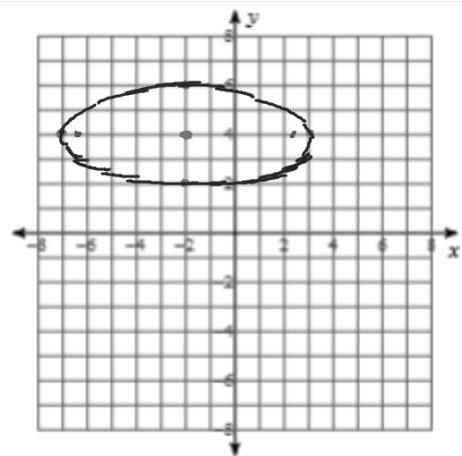
$$\frac{(x+2)^2}{25} + \frac{(y-4)^2}{4} = 1 \quad a=5 \quad b=2$$

$$c^2 = a^2 - b^2 \\ = 25 - 4 \\ c^2 = 21 \quad c = \sqrt{21}$$

Classify the conic section: Ellipse Center: (-2, 4)

Vertices: (3, 4) (-7, 4) Foci: (-2 \pm \sqrt{21}, 4)

Co-vertices  
(-2, 2) (-2, 6)



2. Find the required information and graph the conic section:  $y = 2x^2 - 8x + 4$

$$(x-h)^2 = 4p(y-k)$$

$$y-4 = 2x^2 - 8x$$

$$2x^2 - 8x = y - 4 + 8$$

$$2(x^2 - 4x + 4)$$

$$2(x-2)^2 = y + 4$$

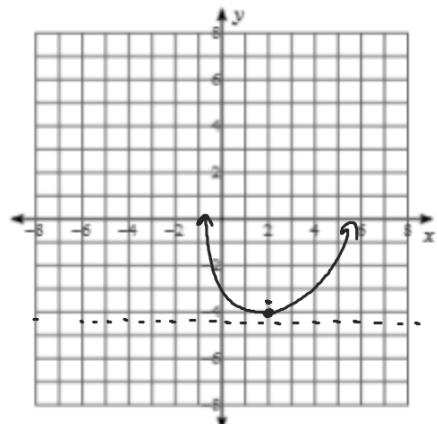
Classify the conic section: Parabola      Vertex: (2, -4)

Focus:  $(2, -3\frac{7}{8})$       Directrix:  $y = -4\frac{1}{8}$

$$(x-2)^2 = \frac{1}{2}(y+4)$$

$$\frac{4p}{4} = \frac{1}{2} \quad \frac{1}{2} = \frac{1}{2} \cdot \frac{1}{4}$$

$$p = \frac{1}{8}$$



3. Find the required information. Then graph the conic section.

$$\frac{(x-2)^2}{9} - \frac{(y-1)^2}{16} = 1$$

$$a = 3$$

$$b = 4$$

$$c^2 = a^2 + b^2$$

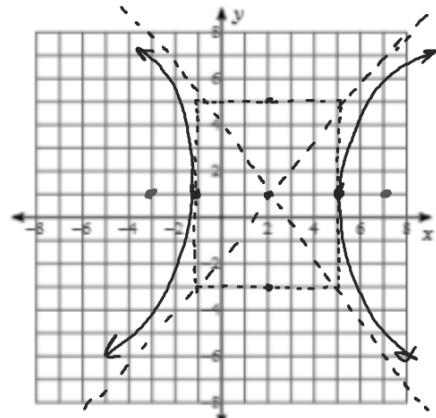
$$c = 5$$

Classify the conic section: Hyperbola Foci: (7, 1) (-3, 1)

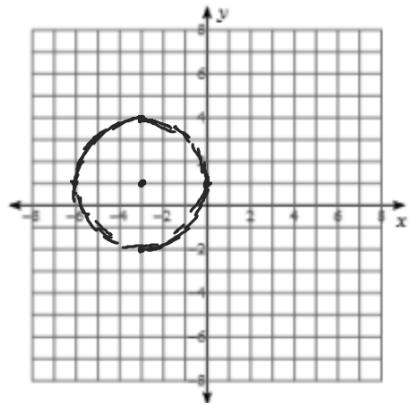
Vertices: (5, 1) (-1, 1) Asymptotes: \_\_\_\_\_ Center: (2, 1)

Co-vertices  
(2, 5) (2, -3)

$$y = \pm \frac{4}{3}(x-2) + 1$$



5. Find the required information and graph:  $(x + 3)^2 + (y - 1)^2 = 9$



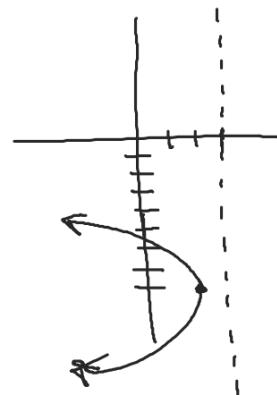
Classify the conic section: Circle      Center: (-3, 1)      Radius: 3

Write the equation of the parabola in vertex form that has the following information:

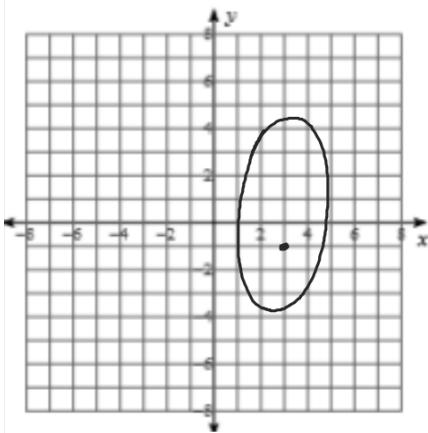
**Vertex:** (2, -8)    **Directrix:**  $x = 3$

$$(y - 1)^2 = 4p(x - h) \quad P = -1$$

$$(y + 8)^2 = -4(x - 2) \quad 4p = -4$$



Find the required information and graph:  $7x^2 + 3y^2 - 42x + 6y - 39 = 0$



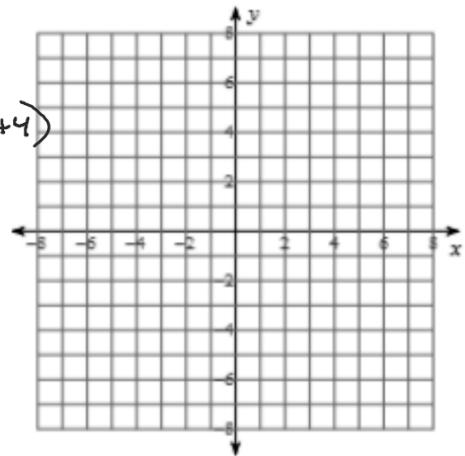
$$\begin{aligned}
 & 7x^2 - 42x + 3y^2 + 6y = 39 \\
 & 7(x^2 - 6x + 9) + 3(y^2 + 2y + 1) = 39 + 63 + 3 \\
 & \frac{7(x-3)^2}{105} + \frac{3(y+1)^2}{105} = \frac{105}{105} \quad a = \sqrt{35} \\
 & \frac{(x-3)^2}{15} + \frac{(y+1)^2}{35} = 1 \quad b = \sqrt{15} \\
 & \text{Classify the conic section: } \underline{\text{Ellipse}} \quad \text{Center: } \underline{(3, -1)} \quad c = \sqrt{20} \\
 & \text{Vertices: } \underline{(3, -1 \pm \sqrt{35})} \quad \text{Foci: } \underline{(3, -1 \pm \sqrt{20})} \\
 & \text{Co-vertices: } \underline{(3 \pm \sqrt{15}, -1)}
 \end{aligned}$$

8. Find the required information and graph the conic section:

$$\begin{aligned} 4y^2 - 32y &= -x - 68 \\ 4(y^2 - 8y + 16) &= -x - 68 + 64 \\ 4(y-4)^2 &= -x - 4 \\ 4(y-4)^2 &= -(x+4) \end{aligned}$$

Classify the conic section: Parabola Vertex:  $(-4, 4)$

Focus:  $(-4\frac{1}{16}, 4)$  Directrix:  $y = -3\frac{15}{16}$



$$4p = -\frac{1}{4}$$

$$p = -\frac{1}{16}$$

$$-\frac{1}{4} + \frac{1}{16}$$

$$-\frac{3}{16} + \frac{1}{16}$$

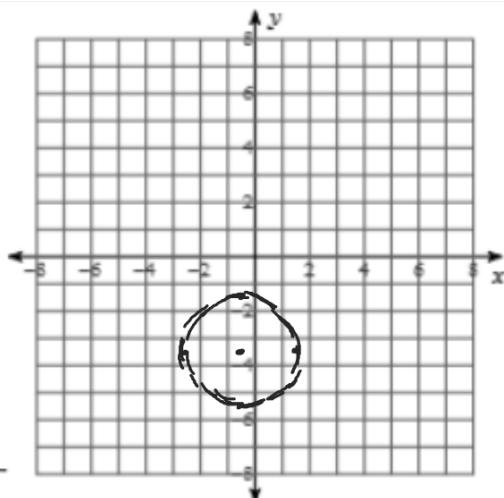
10. Find the required information and graph:

$$2x^2 + 2y^2 + 2x + 14y + 17 = 0$$

$$\begin{aligned}2(x^2 + x + \frac{1}{4}) + 2(y^2 + 7y + \frac{49}{4}) &= -17 + \frac{1}{2} + \frac{49}{2} \\-17 + \frac{50}{2} &= -17 + 25\end{aligned}$$

$$\begin{aligned}2(x + \frac{1}{2})^2 + 2(y + \frac{7}{2})^2 &= 8 \\(x + \frac{1}{2})^2 + (y + \frac{7}{2})^2 &= 4\end{aligned}$$

Classify the conic section: Circle      Center:  $(-\frac{1}{2}, -\frac{7}{2})$   
 $(-0.5, -3.5)$

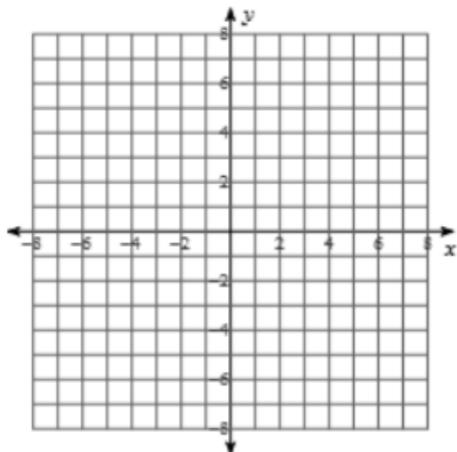


11. Find the required information. Then graph the conic section.

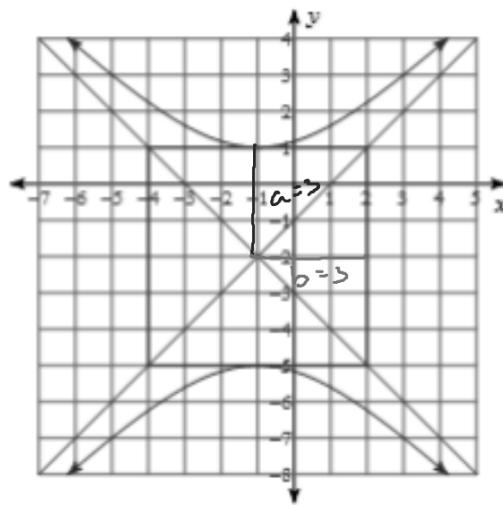
$$-9x^2 + 4y^2 - 18x + 16y - 29 = 0$$

Classify the conic section: \_\_\_\_\_ Foci: \_\_\_\_\_

Vertices: \_\_\_\_\_ Asymptotes: \_\_\_\_\_ Center: \_\_\_\_\_



Write the equation of the hyperbola shown.



Center  $(-1, -2)$

$$a = 3$$

$$b = 3$$

$$\frac{(y+2)^2}{9} - \frac{(x+1)^2}{9} = 1$$

13. Write the equation of the hyperbola in vertex form  
that has the following information:

**Vertices:**  $(9, 12)$  and  $(9, -18)$

**Foci:**  $(9, -3 + \sqrt{229})$  and  $(9, -3 - \sqrt{229})$

Write the equation of the circle in standard form given the endpoints of the diameter: (-12, 10) and (-18, 12).

Center (midpt

$$\left( \frac{-12 + (-18)}{2}, \frac{10 + 12}{2} \right)$$

$$(-15, 11)$$

$$(x+15)^2 + (y-11)^2 = 10$$

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$\sqrt{(-15 + 12)^2 + (11 - 10)^2}$$

$$\sqrt{(-3)^2 + (1)^2}$$

$$\sqrt{9 + 1}$$

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Use the information provided to write the equation of the ellipse in standard form.

**Center:**  $(-9, -5)$     **Vertex:**  $(-9, -16)$     **Focus:**  $(-9, -5 + 6\sqrt{2})$

**t III: Find the equation for 16-20: { Hint: Graph to help find the equation }**

Center (7, 3)      Vertex (7, 9)      Focus (7, -2)

Focus (12, 8)    Directrix:  $x = -2$

